Image Processing and Computer Graphics

Lighting

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Motivation

- modeling of visual phenomena
  - light is emitted by light sources, e.g. sun or lamp
  - light interacts with objects
    - light is absorbed or scattered (reflected) at surfaces
  - light is absorbed by a sensor, e.g. human eye or camera

[Akenine-Möller et al.]
Outline

- light
- color
- lighting models
- shading models
Light

- modeled as
  - electromagnetic waves, radiation
  - photons
  - geometric rays
- photons
  - particles
  - characterized by wavelength
    (perceived as color in the visible spectrum)
  - carry energy
    (inversely proportional to the wavelength)
  - travel along a straight line at the speed of light
Radiometric Quantities

- **radiant energy** $Q$
  - photons have some radiant energy

- **radiant flux** $\Phi$, **radiant power** $P$
  - rate of flow of radiant energy per unit time: $\Phi = \frac{dQ}{dt}$
  - e.g., overall energy of photons emitted by a source per time

- **flux density** (irradiance, radiant exitance)
  - radiant flux per unit area: $E = \frac{d\Phi}{dA}$
  - rate at which radiation is incident on, or exiting a flat surface area $dA$
  - describes strength of radiation with respect to a surface area
  - no directional information
Radiometric Quantities

Irradiance

- Irradiance measures the overall radiant flux $\Phi$ (light flow, photons per unit time) into a surface element.

[Kevin Boulanger, Ph.D. thesis]
Radiometric Quantities

Radiant Intensity

- radiant intensity
  - radiant flux per unit solid angle: \( I = \frac{d\Phi}{d\omega} \)
  - radiant flux \( \Phi \) (light flow, photons per unit time) incident on, emerging from, or passing through a point in a certain direction

[Kevin Boulanger, Ph.D. thesis]
Solid Angle

- 2D angle in 3D space
- measured in steradians
  - A steradian is the solid angle subtended at the center of a sphere of radius \( r \) by a portion of the sphere surface with area \( A = r^2 \).

\[
d\omega = \frac{dA}{r^2}
\]

[Wikipedia: Solid angle]
Radiometric Quantities

Radiant Intensity

- light source with direction-dependent radiant intensities

[Wikipedia: Strahlendichte]
Inverse Square Law

- point light source with radiant intensity $I$ in direction $\omega$
- irradiance along a ray in direction $\omega$ is inversely proportional to the square of the distance $r$ from the source $E = \frac{I}{r^2}$
- the number of photons emitted in direction $d\omega$ and hitting surface area $dA$ at distance $r$ is inversely proportional to $r^2$
- the area subtended by a solid angle is proportional to $r^2$
- $E = \frac{d\Phi}{dA} = \frac{d\Phi}{r^2 d\omega} = \frac{I}{r^2}$

[Wikipedia: Inverse Square Law]
Radiometric Quantities

Radiance

- radiance
  - radiant flux per unit solid angle per unit projected area incident on, emerging from, passing through a surface element in a certain direction:
  \[
  L = \frac{d^2 \Phi}{dA_p \, d\omega} = \frac{d^2 \Phi}{dA \, \cos \theta \, d\omega}
  \]
- describes strength and direction of radiation
- constant radiance in all directions corresponds to a radiant intensity that is proportional to \(\cos \theta\), but constant radiant intensity results in different radiance
Radiance and Sensors

- **Radiance**
  - is measured by sensors
  - is computed in computer-generated images
  - is preserved along lines in space
  - does not change with distance

A sensor with a small area receives light from a small set of directions, i.e. radiance

Idealized graphics model of an imaging sensor

[Akenine-Möller et al.]
Conservation of Radiance

- outgoing flux from $\text{d}A_1$ into direction $r_{12}$
  \[ d^2\Phi_1 = L_1 \cdot \cos \beta_1 \cdot \text{d}A_1 \cdot \text{d}\omega_1 \]
  \[ d\omega_1 = \cos \beta_2 \cdot \text{d}A_2 \cdot r^{-2} \]
  \[ d^2\Phi_1 = \frac{L_1 \cdot \cos \beta_1 \cdot \cos \beta_2 \cdot \text{d}A_1 \cdot \text{d}A_2}{r^2} \]

- incoming flux to $\text{d}A_2$ from direction $-r_{12}$
  \[ d^2\Phi_2 = L_2 \cdot \cos \beta_2 \cdot \text{d}A_2 \cdot \text{d}\omega_2 = \frac{L_2 \cdot \cos \beta_1 \cdot \cos \beta_2 \cdot \text{d}A_1 \cdot \text{d}A_2}{r^2} \]

- if flux is preserved, the radiance does not change
  \[ d^2\Phi_1 = d^2\Phi_2 \Leftrightarrow L_1 = L_2 \]

[Wikipedia: Strahldichte]
Radiance and Sensors

- three imaginary photos of the Sun from different distances

- radiance in a pixel does not depend on the distance
  - irradiance of a pixel received from dA on the Sun is proportional to $1/r^2$
  - dA on the Sun captured by a pixel in directions $d\omega$ is proportional to $r^2$

## Radiometric Quantities

<table>
<thead>
<tr>
<th>Radiometric Quantity</th>
<th>Symbol</th>
<th>Unit</th>
<th>German</th>
</tr>
</thead>
<tbody>
<tr>
<td>Radiant Energy</td>
<td>Q</td>
<td>J</td>
<td>Strahlungsenergie</td>
</tr>
<tr>
<td>Radiant Flux</td>
<td>Φ</td>
<td>W</td>
<td>Strahlungsfluss</td>
</tr>
<tr>
<td>Flux Density (Irradiance, Radiant Exitance)</td>
<td>E</td>
<td>W·m⁻²</td>
<td>Strahlungsstromdichte</td>
</tr>
<tr>
<td>Radiant Intensity</td>
<td>I</td>
<td>W·sr⁻¹</td>
<td>Strahlungsstärke / Strahlungsintensität</td>
</tr>
<tr>
<td>Radiance</td>
<td>L</td>
<td>W·m⁻²·sr⁻¹</td>
<td>Strahldichte</td>
</tr>
</tbody>
</table>
## Photometric / Radiometric Quantities

<table>
<thead>
<tr>
<th>Fotometrische Größe</th>
<th>Einheit</th>
<th>Strahlungsgröße</th>
<th>Einheit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lichtmenge</td>
<td>lm · s</td>
<td>Strahlungsenergie</td>
<td>J</td>
</tr>
<tr>
<td>Lichtstrom</td>
<td>lm</td>
<td>Strahlungsfluss</td>
<td>W</td>
</tr>
<tr>
<td>Beleuchtungsstärke</td>
<td>lx</td>
<td>Bestrahlungsstärke</td>
<td>W · m⁻²</td>
</tr>
<tr>
<td>Lichtausstrahlung</td>
<td>lm · m⁻²</td>
<td>Ausstrahlung</td>
<td></td>
</tr>
<tr>
<td>Lichtstärke</td>
<td>cd</td>
<td>Strahlungsstärke /</td>
<td>W · sr⁻¹</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Strahlungsintensität</td>
<td></td>
</tr>
<tr>
<td>Leuchtdichte</td>
<td>cd · m⁻²</td>
<td>Strahldichte</td>
<td>W · m⁻² · sr⁻¹</td>
</tr>
</tbody>
</table>
Summary

- light consists of photons
- irradiance and radiant exitance describe the flux, i.e. the number of photons per time, into or from a surface per area
- radiant intensity is flux into a direction per solid angle
- radiance describes the flow into or from a surface from a certain direction per area per solid angle
- radiance is measured in sensors
- irradiance of a surface is inversely proportional to its squared distance for a point source with a certain radiant intensity
- radiance is preserved along straight (empty) lines
Outline

- light
- color
- lighting models
- shading models
Visible Spectrum

- photons are characterized by a wavelength within the visible spectrum from 390 nm to 750 nm
- light consists of a set of photons
- the distribution of wavelengths within this set is referred to as the spectrum of light
- spectra are perceived as colors
Visible Spectrum

- if the spectrum consists of a dominant wavelength, humans perceive a "rainbow" color (monochromatic)

- equally distributed wavelengths are perceived as a shade of gray, ranging from black to white (achromatic)

- otherwise, colors "mixed from rainbow colors" are perceived (chromatic)

This spectrum corresponds to a ripe brown banana under white light

[Akenine-Möller et al.]
Human Eye

- is sensitive to radiation within the visible spectrum
- has sensors for day and night vision
  - three types of cones (Zapfen) for photopic (day) vision
  - rods (Stäbchen) for scotopic (night) vision
- perceived light is the radiation spectrum weighted with absorption spectra (sensitivity) of the eye
- in daylight, three cone signals are interpreted by the brain

Normalised absorption spectra of human cone (S,M,L) and rod (R) cells. Cones are sensitive to blue, green, red.

[Wikipedia: Trichromacy]
CIE Color Space

- XYZ color space
  - created by the Int. Commission on Illumination CIE in 1931

\[
X = \int_{\lambda} I(\lambda) \bar{x}(\lambda) d\lambda \\
Y = \int_{\lambda} I(\lambda) \bar{y}(\lambda) d\lambda \\
Z = \int_{\lambda} I(\lambda) \bar{z}(\lambda) d\lambda
\]

- spectrum I is represented by X, Y, Z
  - given the color-matching functions \( \bar{x} \), \( \bar{y} \), \( \bar{z} \)
  - the color-matching functions correspond to the spectral sensitivities of the cones of a standard observer

[Wikipedia: CIE 1931 color space]
CIE xy Chromaticity Diagram

- XYZ represents color and brightness / luminance
- two values are sufficient to represent color
  \[ x = \frac{X}{X+Y+Z} \]
  \[ y = \frac{Y}{X+Y+Z} \]
- monochromatic colors are on the boundary
- the center is achromatic

[Wikipedia: CIE 1931 color space]
Display Devices

- use three primary colors
  - an example is indicated in the diagram
- can only reproduce colors within the spanned triangle (gamut)
- → colors outside the gamut are not properly displayed on a monitor

[Akenine-Möller et al.]
**RGB Color Space**

- three primaries: red, green, blue

![RGB Color Space Diagram](image_url)
RGB Color Space

Lights and Objects

- light source color
  - e.g., yellow light (1, 1, 0)
  - emits a spectrum with maximum red and green components
  - the spectrum does not contain any blue
  - the RGB values describe the amount of the respective color component in the emitted light

- object color
  - e.g., yellow object (1, 1, 0)
  - perfectly reflects red and green comp. of the incoming light
  - perfectly absorbs the blue component of the incoming light
  - the RGB values describe how much of the respective incoming color component is reflected ("one minus value" describes how much is absorbed)
Summary

- the distribution of wavelengths within the flux of the perceived radiance is referred to as the spectrum of light
- spectra are weighted with absorption spectra of the eye and perceived as colors
- three cone types for daylight vision motivate XYZ space
- RGB space is often used for display devices
- colors of display devices are restricted to a gamut that does not contain all perceivable colors
Outline

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Motivation

- compute the interaction of objects with light based on an illumination model (reflection model, lighting model)
- account for a variety of light sources and material properties
- but, keep it fast
  - only use local information per vertex / fragment
    - light source color, direction, and distance
    - object color (material) and surface normal
    - viewer direction
- interaction between objects is neglected
- interreflections among objects, occluded light sources or areal light sources are not handled
Outline

- light
- color
- lighting models
  - diffuse reflection
  - specular reflection
  - ambient light
  - Phong illumination model
  - miscellaneous
- shading models
### Diffuse vs. Specular

- **diffuse**
  - incident light is reflected into many different directions
  - matte surfaces
- **specular (mirror-like)**
  - incident light is reflected into a dominant direction (perceived as small intense specular highlight)
  - shiny surfaces
- **diffuse and specular reflection are material properties**

[Wikipedia: Phong Shading]
Diffuse vs. Specular

- paper and marble have diffuse reflecting surfaces
- in general, materials are characterized by a combination of diffuse and specular reflection

incident and reflected radiant flux of a diffuse and specular reflecting surface

[Wikipedia: Diffuse Reflection]
**Lambert's Cosine Law**

- computation of diffuse reflection is governed by Lambert's cosine law
- radiant intensity reflected from a "Lambertian" (matte, diffuse) surface is proportional to the cosine of the angle between view direction and surface normal $n$

$$I \cdot \cos \theta = I$$

[Wikipedia: Lambert's Cosine Law]
Lambert's Cosine Law

Radiant intensity $I$ and flux $\Phi$ are proportional to the cosine of the angle $\theta$.

$$d\Phi_1 = I \cdot \cos \theta \cdot d\omega = I \cdot d\omega$$

$$d\Phi_2 = I \cdot \cos \theta \cdot d\omega$$

$L$ measured at a sensor is independent from angle $\theta$ and distance.

Computation of diffuse reflection is independent from the viewer direction and distance.

$$L = \frac{I \cdot d\omega}{dA_o \cdot d\omega_o \cdot \cos \theta}$$

$dA_o$ is the size of the sensor. $d\omega_o \cos \theta$ is the solid angle subtended by $dA$.

[Wikipedia: Lambert's Cosine Law]

[University of Freiburg – Computer Science Department – Computer Graphics - 34]
Lambert's Cosine Law

- irradiance on an oriented surface patch above a Lambertian surface is constant

\[ E = \frac{\Phi}{dA} = \frac{\Phi \cos \theta}{dA \cos \theta} \]
Lambert's Cosine Law

- irradiance on a surface is proportional to the cosine of the angle between surface normal $n$ and light source direction $l$ (also referred to as Lambert's Cosine Law)

$$E = \frac{\Phi}{A \cos \theta} = \frac{\Phi}{A} \cos \theta = E_L \cos \theta$$
Diffuse Lighting

Irradiance of the object surface (yellow) depends on the angle between light source (red) direction and surface normal.

Radiant intensity of the surface depends on the angle between radiation direction and surface normal.

[Wikipedia: Lambertsches Gesetz]
Diffuse Lighting

- radiance (RGB) is computed as $L_{\text{diff}} = \frac{1}{\pi} \cdot c_{\text{diff}} \otimes E_L \cdot \cos \theta$
  - $\otimes$ denotes component-wise multiplication, 
    $(a, b, c) \otimes (d, e, f) = (a \cdot d, b \cdot e, c \cdot f)$
  - $1/\pi$ is a normalization coeff. motivated by energy conservation: light is reflected in all directions of a hemisphere and the viewer only receives a portion of the reflected light

- in implementations,
  - $\pi$ is usually incorporated in $E_L$
  - $\cos \theta$ is computed as the dot product of the normalized light direction and the normalized surface normal
    $L_{\text{diff}} = c_{\text{diff}} \otimes E_L \cdot \max(0, n \cdot l)$
  - neg. values $n \cdot l$ correspond to illuminating the back of a surface, the max-function is often omitted for readability
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  - specular reflection
  - ambient light
  - Phong illumination model
  - miscellaneous
- shading models
Specular Reflection

- perceived radiance depends on the viewing direction
  - maximum radiance, if the viewer direction v corresponds to the reflection direction r or, if the halfway vector h corresponds to the surface normal

- Phong model
  \[ L_{\text{spec}} = c_{\text{spec}} \otimes E_L \cdot (\max(0, v \cdot r))^m \]

  \( c_{\text{spec}} = (1,1,1) \) is popular for the specular color, since the color of specular reflection converges to the color of the incident light. The exponent m characterizes the size of the specular highlight. Maximum radiance is not influenced.

- Blinn-Phong model
  \[ L_{\text{spec}} = c_{\text{spec}} \otimes E_L \cdot (\max(0, n \cdot h))^m \]

  Standard specular term in OpenGL (prior to OpenGL 3.1)

  [Wikipedia: Blinn-Phong shading model]
Specular Reflection Implementation

- Phong model
  - requires the reflection vector $r$ which can be computed from $n$ and $l$
    \[ r = 2(n \cdot l)n - l \]

- Blinn-Phong model
  - requires the halfway vector $h$ which can be computed from $l$ and $v$
    \[ h = \frac{l + v}{\|l + v\|} \]

[Wikipedia: Blinn-Phong shading model]
Reflection Vector

- computed with light source direction $l$ and surface normal $n$

\[ r + l = 2 \cdot \cos \theta \cdot n \]

\[ \cos \theta = l \cdot n \]

\[ r = 2 \cdot (l \cdot n) \cdot n - l \]

- $l$ and $n$ have to be normalized
- $r$ is normalized
Non-normalized Blinn-Phong

- Phong and Blinn-Phong do not account for energy preservation
- radiance depends on angle $\theta$ and exponent $m$
- radiant exitance from the surface depends on $m$

angle $\theta$ between $v$ and $r$ (Phong)
or $n$ and $h$ (Blinn-Phong)

[Akenine-Möller et al.]
Normalized Blinn-Phong

- normalized Blinn-Phong versions account for energy conservation

  e.g.

  \[ L_{\text{spec}} = \frac{m+8}{8\pi} \cdot c_{\text{spec}} \otimes E_L \cdot (n \cdot l) \cdot (n \cdot h)^m \]

  [Akenine-Möller et al., Real-time Rendering]

- considers angle-dependent irradiance

- considers growing maximum radiance for growing exponent \( m \)

- radiant exitance is approximately constant for varying \( m \)

[Akenine-Möller et al.]
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 Ambient Light

- diffuse and specular reflection are modeled for directional light from a point light source or from parallel light (point light source at infinity)
- ambient light is an approx. for indirect light sources
  - reflected light from objects illuminates other objects
  - all objects in the hemisphere seen from a surface act as light source for this surface
- this effect is generally approximated by a constant, object-dependant offset $L_{\text{amb}} = c_{\text{amb}} \otimes E_{\text{amb}}$
- $c_{\text{amb}}$ usually corresponds to $c_{\text{diff}}$, $E_{\text{amb}}$ represents ambient illumination, e.g. the dominant object color
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Phong Illumination Model

- combines ambient, diffuse, and specular components
  \[ L_p = c_{amb} \otimes E_{amb} + c_{diff} \otimes E_{diff} \cdot (n \cdot l) + c_{spec} \otimes E_{spec} \cdot (r \cdot v)^m \]

- Phong allows to set different light colors for different components (which is not physically motivated)

- a useful parameter setting could be
  \[ L_p = E_{amb} \otimes c_{obj} + E_{light} \otimes (c_{obj} \cdot (n \cdot l) + c_{spec} \cdot (r \cdot v)^m) \]

- multiple light sources, e. g.
  \[ L_p = c_{amb} \otimes E_{amb} + \sum_{light} E_{light} \otimes (c_{diff} \cdot (n \cdot l) + c_{spec} \cdot (r \cdot v)^m) \]

- max-functions are omitted. n, l, r, v are normalized. Max values for RGB comp. of \( L_p \) have to be considered.
Phong Illumination Model

- parameters (material and light colors) can be used to adapt the ratios of ambient, diffuse, and specular reflection components

[Wikipedia: Phong shading]
Phong Illumination Model


University of Freiburg – Computer Science Department – Computer Graphics - 50
Blinn-Phong Illumination Model

- non-normalized Blinn-Phong
  \[ \mathbf{L}_{bp} = c_{amb} \otimes \mathbf{E}_{amb} + c_{diff} \otimes \mathbf{E}_{diff} \cdot (\mathbf{n} \cdot \mathbf{l}) + c_{spec} \otimes \mathbf{E}_{spec} \cdot (\mathbf{h} \cdot \mathbf{n})^m \]

- parameter setting and multiple light sources (see Phong)

- normalized Blinn-Phong, e.g.
  \[ \mathbf{L}_{nbp} = \mathbf{E}_{amb} \otimes \mathbf{c}_{amb} + \left( \frac{1}{\pi} \mathbf{c}_{diff} + \frac{m+8}{8\pi} \cdot \mathbf{c}_{spec} \cdot (\mathbf{h} \cdot \mathbf{n})^m \right) \otimes \mathbf{E}_L \cdot (\mathbf{l} \cdot \mathbf{n}) \]

- in implementations, the normalization coefficient can be incorporated into \( c_{diff} \) and \( c_{spec} \)
  \[ \mathbf{L}_{nbp} = \mathbf{E}_{amb} \otimes \mathbf{c}_{amb} + \left( \mathbf{c}_{diff} + \mathbf{c}_{spec} \cdot (\mathbf{h} \cdot \mathbf{n})^m \right) \otimes \mathbf{E}_L \cdot (\mathbf{l} \cdot \mathbf{n}) \]
Phong vs. Blinn-Phong

- Phong (left) and Blinn-Phong (right)
- Highlights on flat surfaces are more realistic with Blinn-Phong
- Blinn-Phong (top) and normalized Blinn-Phong (bottom)
- Maximum radiance of the highlight for varying $m$ is constant for Blinn-Phong

[Akenine-Möller et al.]
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Considering Distances

- between object surface and light source
  - irradiance of a surface illuminated by a point light source is inversely proportional to the squared distance from the surface to the light source
  - light source attenuation

- between object surface and viewer
  - atmospheric effects, e.g. fog, influence the visibility of objects
  - visibility refers to the transparency of air
  - if air is transparent, objects are clearly visible
  - in less transparent air, fog particles absorb some flux and scatter additional flux towards the viewer
  - in low visibility, radiance converges to a "fog color"
Light Source Attenuation

- for a point light source with position \( \mathbf{l} = (l_x, l_y, l_z, 1)^T \), the distance \( d \) from the light source to a surface point \( \mathbf{p} = (p_x, p_y, p_z, 1)^T \) can be considered in the irradiance of the light source
  \[ d = \| \mathbf{p} - \mathbf{l} \| \]
  \[ E_{\text{att}} = \frac{1}{k_c + k_l \cdot d + k_q \cdot d^2} I_{\text{light}} \]

- this is motivated by \( E_{\text{light}} = \frac{I_{\text{light}}}{d^2} \)

  (irradiance \( E \) is inversely proportional to the squared distance from the light source with radiant intensity \( I \))

- \( k_c, k_l, k_q \) are user-defined parameters
Fog

- fog is approximated by a linear combination of the computed radiance \( L \) and a fog color \( c_{\text{fog}} \)
- \( d \) is the distance of the surface point to the viewer (its z-component, i.e. depth value)

\[
L_{\text{fog}} = f(d) \cdot L + (1 - f(d)) \cdot c_{\text{fog}}
\]

- \( 0 \leq f(d) \leq 1 \) is a function that describes the visibility
  - \( f(d) = 1 : \) max visibility (object color is unaffected)
  - \( f(d) = 0 : \) min visibility (object color is changed to fog color)
  - e.g. \( f(d) = \frac{d_{\text{end}} - d}{d_{\text{end}} - d_{\text{start}}} \)  \( f(d) = e^{-\text{density} \cdot d} \)

linear fog: starts at \( d_{\text{start}} \), minimum visibility at \( d_{\text{end}} \). Clamped to [0..1].

exponential fog
Attenuation and Fog


[http://www.gamedev.net/topic/541383-typical-light-attenuation-coefficients/]
Light Sources

- positional light source at position \( \mathbf{l} = (l_x, l_y, l_z, 1)^T \)
- directional light source with direction \( \mathbf{l} = (l_x, l_y, l_z, 0)^T \)
- spotlight
    - positional light with flux into restricted directions
    - e.g. \( \mathbf{E}_{\text{spot}} = I_{\text{light}} \cdot \max(-l \cdot s, 0)^{m_{\text{spot}}} \)
    - \( I_{\text{light}} \) is the maximum radiant intensity of the spotlight in direction \( s \)
    - \( l \) is the direction to the light
    - \( m_{\text{spot}} \) is user-defined to adapt the fall-off rate of the radiant intensity with respect to the cosine of the angle between \(-l\) and \(s\)
    - \( I_{\text{light}} \) should be divided by some squared distance)
Spotlight

[http://www.ozone3d.net/tutorials/gls_lighting_phong_p3.php]
Summary

- the class of Phong lighting models considers
  - diffuse and specular reflection
  - ambient illumination
- the lighting models are efficient to compute as they only consider local information, e.g. surface normal, light source direction, viewer direction, ...
- improved variants consider energy conservation and lead to more realistic specular highlights
- additionally, distances to the viewer and the light source can be considered
- various types of light sources can be realized
Outline

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- shading models
Introduction

- shading models specify whether the lighting model is evaluated per vertex or per fragment
- if evaluated per vertex, the shading model specifies whether the resulting vertex colors are interpolated across a primitive or not
- if evaluated per fragment, surface normals are interpolated across a primitive
Shading Models

- flat shading (constant shading)
  - evaluation of the lighting model per vertex
  - primitives are colored with the color of one specific vertex

- Gouraud shading
  - evaluation of the lighting model per vertex
  - primitives are colored by bilinear interpolation of vertex colors

- Phong shading
  - bilinear interpolation of vertex normals during rasterization
  - evaluation of the lighting model per fragment
Flat vs. Phong

[Wikipedia: Phong shading]
Gouraud Shading

Low polygon count

Highlight is poorly resolved.
Mach band effect.

High polygon count

[Wikipedia: Gouraud shading]
Mach Band Effect

- Mach bands are illusions due to our neural processing.

The bright bands at 45 degrees and 135 degrees are illusory.

The intensity inside each square is the same.
Shading Models

- flat shading (constant shading)
  - simplest, fastest
- Gouraud shading
  - more realistic than flat shading for the same tessellation
  - suffers from Mach band effect
  - local highlights are not resolved, if the highlight is not captured by a vertex
- Phong shading
  - highest quality, most expensive
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